

**PG Department of Mathematics**  
**QUESTION BANK**

**TOPOLOGY-II**

1. a) Define Lindloff Space. Prove that every Second countable axiom space is a Lindloff space.  
b) Prove that every separable metric space is second axiom space.
2. a) Define  $T_0$  space. Prove that  $T_0$  space the closure district points are district and conversely.  
b) Define limit point compactness. If every countable open cover of  $X$  has a finite sub cover then  $X$  is countably compact.
3. a) Define Sequential Compact. Prove that a countably metric space  $(X, d)$  is sequential compact.  
b) Define Projection Mapping. Show that Projection maps are continuous and open further the product topology is smallest topology with respect to which projections are continuous
4. a) The product  $X \times Y$  of two topological space  $X$  and  $Y$  is Housdroff or  $T_2$  iff  $X$  and  $Y$  are  $T_2$ .  
b) Every metric space is a  $T_2$  space.
5. a) Define Housdroff Space. And hence prove the hereditary property for it.  
b) Prove that Metric space is  $T_3$  space.
6. State and Prove Urysohn's Lemma.
7. a) Prove that every regular second countable  $T_1$  space is Metrizable.  
b) A compact Housdroff space is normal.
8. a) A regular Lindeloff space is normal.  
b) State and prove Tietz extension Theorem.